## DMC 013, Research Methodology, Sessional Exam - June 07, 2021, 12:01 pm to 2:00 pm Max score = 20 (Q1 = 10, Q2 = 2x5 = 10)

Q1 In the following test of hypothesis, the population variance  $\sigma^2$  is <u>not</u> known, and hence the standard Gaussian based *Z* statistic cannot be used. Devise an appropriate strategy for testing the hypothesis.

Let *X* (in mm) equal the growth in 15 days of a tumour induced in a mouse. Assume that the distribution of  $X \sim N(\mu, \sigma^2)$ . You have to test the hypothesis if the average tutor size is 4 mm or not. Use the level of significance of the test  $\alpha = 0.10$  and the following data,

 $X = \{4.20, 4.90, 3.50, 2.40, 3.30, 3.75, 4.75, 5.95, 5.95\}$ 

Clearly state the null and alternate hypothesis, the test statistic you are using for the test and your inference. You may use any of the following information:

 $z_{0.1}(\sigma/\sqrt{9}) = 0.039, \ z_{0.05}(\sigma/\sqrt{9}) = 0.012, \ t_{0.05}(8) = 1.86, \ t_{0.1}(8) = 1.4, \ t_{0.05}(9) = 1.83, \ t_{0.1}(9) = 1.38$ 

- Q2 i) State the Bayes' theorem.
  - ii) Name two sampling distributions. Which of them is used for ANOVA?
  - iii) State any two of the three axioms of probability.
  - iv) Name two discrete probability distributions.
  - v) Which probability distribution has the same value for expectation and variance?